PAPER

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Non-Maxwellian electron energy probability functions in the plume of a SPT-100 Hall thruster

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Abstract
We present measurements of the electron density, the effective electron temperature, the plasma potential, and the electron energy probability function (EEPF) in the plume of a 1.5 kW-class SPT-100 Hall thruster, derived from cylindrical Langmuir probe measurements. The measurements were taken on the plume axis at distances between 550 and 1550 mm from the thruster exit plane, and at different angles from the plume axis at 550 mm for three operating points of the thruster, characterized by different discharge voltages and mass flow rates. The bulk of the electron population can be approximated as a Maxwellian distribution, but the measured distributions were seen to decline faster at higher energy. The measured EEPFs were best modelled with a general EEPF with an exponent $\alpha$ between 1.2 and 1.5, and their axial and angular characteristics were studied for the different operating points of the thruster. As a result, the exponent $\alpha$ from the fitted distribution was seen to be almost constant as a function of the axial distance along the plume, as well as across the angles. However, the exponent $\alpha$ was seen to be affected by the mass flow rate, suggesting a possible relationship with the collision rate, especially close to the thruster exit. The ratio of the specific heats, the $\gamma$ factor, between the measured plasma parameters was found to be lower than the adiabatic value of $5/3$ for each of the thruster settings, indicating the existence of non-trivial kinetic heat fluxes in the near collisionless plume. These results are intended to be used as input and/or testing properties for plume expansion models in further work.

Keywords: EEPF, Hall thruster, plasma plume, electric propulsion

1. Introduction

Electric propulsion is a solid alternative to classical chemical propulsion for both station keeping and orbit raising of spacecraft, as well as for deep space exploration. Hall thrusters are a type of electric thruster in which heavy atoms, typically noble gas such as xenon, are ionized and accelerated using an electric field (Martinez-Sanchez and Pollard 1998, Goebel and Katz 2008, Mazouffre 2016, Boeuf 2017). The ejection of the ions provides thrust to the spacecraft; neutralization of those ions is necessary to avoid payload charging and therefore electrons are also ejected from a cathode.
Both ions and electrons then form the plasma plume expanding from the thruster exhaust. Understanding the plasma environment created by the electric thruster is crucial in order to avoid issues such as energetic ions sputtering the spacecraft structure, direct contamination due to erosion products or impingement of ions nearby of the spacecraft which can induce perturbing forces and torques. Of particular concern with the use of Hall thrusters is the effect of the highly energetic plasma exhaust plume on the surfaces of the spacecraft, in particular the solar arrays. For these reasons, advanced modelling of the plasma plume is required (Roussel et al 1997, 2008, Boyd and Dressler 2002, Beal et al 2004, Sedlák et al 2005, Hu and Wang 2017) in order to improve understanding and provide input for optimizing spacecraft design.

However, proper knowledge of the plasma behaviour in this region is still lacking, with a major missing piece being the cooling mechanism of the electrons as the plume expands, both along its axis and angularly off the plume axis. The cooling of the electrons is linked to the absence of local thermodynamic equilibrium in the low-collisionality plume. In a highly collisional plume, adiabatic cooling from the local thermodynamic equilibrium of the electrons would be expected, whereas in a collisionless plume, most electrons are axially confined by the ambipolar electric field and a purely confined electron species would be isothermal. The actual expansion is more complicated than a middle point between the two cases: part of the electrons escape downstream to neutralize the ion beam, and non-monotonic effective potential barriers may exist. Theoretical work is ongoing in order to provide a solution to this problem (Cichocki et al 2014, 2015, Merino et al 2017) and the presented work aims at providing experimental measurements to support this effort. There have been experimental characterization of Hall thrusters using Langmuir probes, including the very-near-field plume (0–200 mm, Kim et al 1996) and the far-field plume (300–500 mm, Dannenmayer et al 2011, 2012, Dannenmayer and Mazouffre 2013), but reliable measurements beyond 500 mm are scarce.

This article presents new results from a measurement campaign in which cylindrical Langmuir probes were used to measure the key plasma parameters at distances between 500 and 1550 mm from the exit of a SPT-100 (stationary plasma thruster) Hall thruster. The electron density, the effective electron temperature, the plasma potential, and the electron energy probability functions (EEPF) were recorded at multiple axial and angular locations inside the plume far-region of the thruster.

2. Experimental apparatus, method and measurements

Measurements were performed inside a large vacuum chamber (2 m in diameter and 4 m in length) using two cylindrical Langmuir probes (0.2 mm diameter, 5 mm length) oriented parallel to the ion stream lines. The tip of the probes was made of tungsten, with an alumina body shielding the rest of the probe. The first cylindrical Langmuir probe was installed on a translation stage, mounted on a rotating arm, allowing for angular scans at distances from 500 to 750 mm to the thruster exit. The second cylindrical Langmuir probe was mounted on a larger translation stage, providing measurements along the plume axis from 850 to 1550 mm. All measurements were performed in the horizontal plane located at the height of the thruster axis (x = 0 referring to the exit of the thruster), and recorded using a Keithley 2440 sourcemeter sweeping the probe voltage from −15 V to +35 V.

In this article, only measurements performed along the plume axis (from 550 to 1550 mm with respect to the thruster) and angularly from 0.5° to 84.5° (0° being aligned with the thruster axis) at a radial distance of 550 mm are discussed. An overview of the configuration is shown in figure 1, with the location of the discussed measurements indicated in red. These measurements were recorded for three different operating points of the thruster, where the discharge voltage and the mass flow rate of xenon were varied: (300 V, 4 mg s⁻¹), (300 V, 2 mg s⁻¹), and (400 V, 2 mg s⁻¹), respectively. More details on the entire measurement campaign are described in Giono et al (2017).

The Hall thruster employs magnetic fields to achieve propellant acceleration. In the case of the SPT-100 thruster used in this experiment, the magnetic field at the exit plane is around 150 G (15 mT), which is itself about 50 mm from the magnet. Hence, the residual magnetic field from the thruster is below 10 μT in the plume region studied, 500 mm away from the thruster exit. The magnetic field lines around the thruster exit for a similar SPT configuration can be seen in the top-left part of figure 2 from Hagelaar et al (2003). Earth magnetic field is therefore the dominant magnetic field, with an average field strength of 50 μT. For such field strength, and considering an electron temperature of 2 eV, the Larmor radius of the electron is of the order of 100 mm. Such Larmor radius is more than one order of magnitude larger than the Langmuir probe dimension, indicating that the plasma can be considered unmagnetized for the analysis. The pressure inside the vacuum chamber while running the thruster was below 10⁻⁴ Torr during all measurements, and below 10⁻⁶ Torr otherwise. Hence, xenon neutrals were by far the most abundant element inside the chamber when running the
to vary greatly as a function of energy from 1 to 6 eV but becomes constant beyond 6 eV. Based on this, the mean free path of electrons in neutral xenon is larger than 2 m at 2 mg s$^{-1}$ and larger than 1 m at 4 mg s$^{-1}$. Therefore, the plasma inside the plume cannot be considered fully-collisionless, but the average number of collision is not very high either: between 1 and 3 collisions along a 1.5 m distance for ions, and between 0.5 to 1.5 collisions for electrons. As a consequence of this, the electrons are not expected to be in local thermodynamic equilibrium.

The plasma parameters were derived from the Langmuir probe current measurements. First, the plasma potential was determined by locating the maximum of the first derivative of the current $dI/dV$, smoothed using a Blackman window convolution (2 V width) to reduce the fluctuation induced by the measurement noise (Magnus and Gudmundsson 2008). The electron energy distribution function (EEDF) $g_e(E)$ was then derived by taking the second derivative of the current $d^2I/dV^2$ from the plasma potential, following the Druyvesteyn formula (Lieberman and Lichtenberg 2005), using the smoothed $dI/dV$. The Druyvesteyn formula is

$$g_e(E) = \frac{2m_e}{e^2A} \sqrt{\frac{2eE}{m_e}} \frac{d^2I}{dV^2},$$

where $m_e$ is the mass of the electron, $e$ the elementary charge and $A$ the area of the probe. The EEPF $g_p(E)$ is obtained as $g_p(E) = E^{-1/2}g_e(E)$.

The measured EEPFs are presented in figure 2 along the plume axis and in figure 3 for angles off the plume axis, at a 550 mm radial distance. For the three operating conditions, one can see the spatial variation of the EEPF and its relation with the plasma parameters, as its amplitude is proportional to the density and its slope to the electron temperature.

The EEPF peaks at an energy between 0 and 2 eV, which decreases slightly with increased distance and larger angle. In addition, the depletion at low-energy below 1 eV is a measurement artefact due to the finite size of the Langmuir probe (Godyak et al 1992). The noise level can be seen to be about three orders of magnitude lower than the maximum, although values below two orders of magnitude can be seen to be affected by the smoothing of the current derivative.

3. Analysis of the EEPFs

The electron density $n_e$ and effective electron temperature $T_{ee}$ for each measurement can be calculated by integrating the EEDFs (Lieberman and Lichtenberg 2005), as

$$n_e = \int_0^\infty g_e(E) dE \quad T_{ee} = \frac{2}{3n_e} \int_0^\infty E g_e(E) dE,$$

where the effective electron temperature is $T_{ee} = \frac{2}{3} \langle E \rangle$ and $\langle E \rangle$ is the average electron energy. Note that the measured EEDFs were not truncated at the floating potential energy, as the second derivative of the ion current can be considered negligible (Godyak et al 1992). It is worth pointing out that this treatment assumes an isotropic plasma. Fisch et al (2011) and

![Figure 2](image_url)

Figure 2. EEPFs measured along the plume axis, for (a) 300 V, 4 mg s$^{-1}$, (b) 300 V, 2 mg s$^{-1}$ and (c) 400 V, 2 mg s$^{-1}$. Not every axial measurement performed is shown.
Raitses et al (2009) showed that this is not the case close to the thruster exit, as the electrons rotate around the axial direction due to the presence of the magnetic field via a $\mathbf{E} \times \mathbf{B}$ drift. However, in the presented case, the Larmor radius of the electrons at 500 mm is of the same order as the plume width at this distance (two-dimensional maps of the plasma parameters are shown in Giono et al 2017), which suggests that this effect is negligible, as the electrons follow a more kinetic regime. In addition, consistency on the obtained plasma parameters, as well as the recorded EEPFs, can be seen regardless of the distance to the thruster, from 500 to 1550 mm where the magnetic field can be clearly neglected. This also suggests that an isotropic electron population can be considered.

Observations show that the bulk of the electron population has a distribution function close to a Maxwellian (EEPF as a straight line, see figure 4, fitted on the 2 eV wide region following the EEPF maximum). However, for larger electron energy, the distribution rapidly deviates from this Maxwellian distribution: the measured electron energy probability decreases faster than expected from the main Maxwellian population. Such deviation from a Maxwellian distribution was also observed by other authors (Dannenmayer and Mazouffre 2013, Boswell et al 2015, Zhang et al 2016b) at distances much closer to the thruster. Note that the observed EEPFs are also different from the convex bi-Maxwellian case described by Zhang et al (2016a): the depletion observed at higher energy drops faster than for a second Maxwellian distribution.

Further investigation of the non-Maxwellian general case was therefore required. A more general formulation for the EEPF is

$$g_p(\varepsilon) = n_e \frac{3 \alpha}{T_{\text{eff}}} \left[ \frac{2 \Gamma \left( \frac{\alpha}{2} \right) \varepsilon}{3 \Gamma \left( \frac{\alpha}{2} \right) T_{\text{eff}}} \right]^{\frac{\alpha}{2}} \exp \left\{ - \frac{2 \Gamma \left( \frac{\alpha}{2} \right) \varepsilon}{3 \Gamma \left( \frac{\alpha}{2} \right) T_{\text{eff}}} \right\},$$

where $\alpha$ is an exponent describing the curvature of the EEPF (Rundle et al 1973, Gudmundsson 2001). This expression is auto-consistent with equation (2), and reduces to a Maxwellian distribution for $\alpha = 1$, whereas $\alpha = 2$ leads to a Druyvesteyn distribution. A least-square fitting was used to derive the exponent $\alpha$, as well as the electron density and the effective electron temperature, from the measured EEPFs. Only the central part of the EEPF was used for this fitting, from its maximum (i.e. not including the drop at very low energy due to the finite size of the Langmuir probe) to the noise level (i.e. threshold at two orders of magnitude lower than the EEPF maximum). An example of Maxwellian distribution and general distribution fitting is shown in figure 4.

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**Figure 3.** EEPFs measured angularly (at a 550 mm distance from the thruster), for (a) 300 V, 4 mg s$^{-1}$, (b) 300 V, 2 mg s$^{-1}$ and (c) 400 V, 2 mg s$^{-1}$. Not every angular measurement performed is shown.

**Figure 4.** Example of EEPF showing the Maxwellian fitting on the bulk of the distribution, as well as the general fitting. The EEPF is taken along the plume axis at a 1350 mm distance from the thruster exit, for a discharge voltage of 300 V and a mass flow rate of 4 mg s$^{-1}$.
For each of the operating points, three sets of parameters are shown in figures 5 and 6, as a function of the distance along the plume axis, one derived from the measurements, and two from fittings, with a simple Maxwellian and with the general non-Maxwellian, respectively. The measurement value is obtained from integrating the entire experimentally determined EEDF. The derived parameters of the bulk Maxwellian distribution provide an overestimate of $n_e$ and $T_{\text{eff}}$, as the EEPF is observed to decay faster than a Maxwellian at higher energy. On the other hand, the general non-Maxwellian distribution provides very similar plasma parameters as determined from the measurements. Only a small difference can be seen in the electron density, indicating that the loss of low energy electrons observed in the measurement was not significant. All three methods show a similar picture: both electron density and temperature falling off with distance away from the thruster exit. The electron density, shown in figure 5, at 500 mm depends mainly on the flow rate and is $1.2 \times 10^{16}$ m$^{-3}$ at 300 V and 4 mg s$^{-1}$. It falls off with distance and is $2.4 \times 10^{15}$ m$^{-3}$ at 1550 mm from the exit as seen in figure 5(a). The electron density decreases to $3.6 \times 10^{15}$ m$^{-3}$ at 550 mm from the exit when the flow rate is decreased to 2 mg s$^{-1}$ at 300 V. The electron density only increases slightly to $4.5 \times 10^{15}$ m$^{-3}$ at 550 mm from the exit when the discharge voltage is increased to 400 V while the flow rate is 2 mg s$^{-1}$, as seen in figure 5(c). At this flow rate, the electron density drops to $5 \times 10^{14}$ m$^{-3}$ at 1550 mm from the thruster exit. The effective electron temperature seen in figure 6 is slightly higher for the lower flow rate, or 3.0 eV at 550 mm from the thruster exit at 2 mg s$^{-1}$ but drops to 2.4 eV as the flow rate is increased to 4 mg s$^{-1}$ while operating at 300 V. In all cases, $T_{\text{eff}}$ has dropped to roughly 1.7 eV at 1550 mm from the thruster exit. These values are consistent with other studies of a SPT-100 thruster such as Dannenmayer et al (2011). For reference, figure 7 gives the plasma potential along the plume axis for the three operating points of the thruster.
being slightly larger than at 300 V. Finally, one can notice that the shape of the spatial variation of $Y_e$ for a larger mass flow rate of 4 mg s$^{-1}$ is slightly different compared to 2 mg s$^{-1}$.

Figure 8 shows the spatial dependence of the exponent $\alpha$. The exponent $\alpha$ has values between 1.2 and 1.5, which is between Maxwellian and Druyvesteyn distributions. Note that this result for the exponent $\alpha$ could be a consequence of the experimental conditions, i.e., having a much higher neutral density in the background than in space. This will expectedly have a higher collision rate, making the EEPF approach a Maxwellian distribution as the plasma gets closer to its thermodynamic equilibrium. In the better vacuum of space, the results could be different. Nevertheless, the axial and angular variations of the exponent can be discuss meaningfully. Although no significant trends are observed along the plume axis or across the angles, a clear difference is seen depending on the mass flow rate of the thruster. Two conclusions can be drawn from figure 8: first, a higher density of both plasma and neutrals via a higher mass flow rate bring the EEPF closer to a Maxwellian distribution due to the increased collision rate especially closer to the thruster exit, and second, that the proportion of missing high-energy electrons, symbolized by the exponent $\alpha$, is fixed spatially inside the far-plume. An explanation might be due to the higher collision rate in the vicinity of the thruster exit, dictating the proportion of high-energy electrons lost. This property would then not be changed as the plasma propagates in the far-plume, since the collision rate drops to an almost collisionless regime. Investigating how the EEPF properties vary spatially at distances between 0 to 500 mm from the thruster exit would be an interesting future work, but interpreting the results might be more complicated due to the presence of a non-negligible magnetic field in this region.

Establishing a relation between the electron temperature and plasma density is important for the fluid-type models of the plume. In the adiabatic case, the electron density and the electron temperature can be related by the ratio of specific heats $\gamma$ (Boyd and Dressler 2002) as in

$$\left( \frac{n_e}{n_e^0} \right)^\gamma = \left( \frac{T_{eff}}{T_{eff}^0} \right)^{-\frac{1}{\gamma-1}},$$

where $^*$ indicates a reference state. In a collisional gas plume, local thermodynamic equilibrium is expected and a $\gamma$ value of 5/3 is anticipated due to adiabatic cooling. However, in a nearly-collisionless plasma plume, one cannot invoke local thermodynamic equilibrium condition and no simple physical argument leads to 5/3 in a general collisionless plasma expansion; the kinetic response of the electrons must be studied in detail. A $\gamma < 5/3$ in an otherwise isentropic expansion indicates the existence of non-trivial electron kinetic heat-fluxes. The tendency in a collisionless, confined population is for heat fluxes to make the population near-isothermal (i.e. Boltzmann relation). For a partially confined population, $1 < \gamma < 5/3$ is expected. Note that the $\gamma$ parameter is a macroscopic quantity describing the cooling of the plasma. Figure 9 shows the effective electron temperature as a function of electron density along the plume axis for the three operating points. Dots show the measured values and dash lines the best fit for $\gamma$. The electron density and the effective electron temperature were normalized to a common reference point for the fitting of $\gamma$ (axial measurement at 550 mm).
existence of non-trivial kinetic heat-fluxes. One can also notice two different trends on the measured values from the operating point at 4 mg s⁻¹ displayed in figure 9. For this operating point, the six measurement points closer to the thruster exit were not recorded on the same day as the other measurement points further down the plume, which might explain the discontinuity. The γ factor was also derived for the parameters of a fitted Maxwellian distribution and similar values between 1.2 and 1.5 were obtained, indicating that even the bulk of the electron population does not follow an adiabatic cooling law.

5. Conclusion

EEPF measurements in the far-plume of a SPT-100 Hall thruster revealed a loss of high energy electrons compared to the Maxwellian electrons from the bulk of the plasma. The measured EEPFs were best represented by a general EEPF with an exponent α. Best fit for the exponent was between 1.2 and 1.5, placing the measured distributions between a Maxwellian and a Druyvestyn distributions. The exponent α was roughly constant as a function of axial distance and angle, but a clear dependence on the mass flow rate of the thruster was observed, indicating a possible dependence on the collision rate inside the plume, especially close to the thruster exit. A γ parameter around 1.2 was found to link the electron density to the electron temperature, which is smaller than the value for adiabatic cooling of 5/3. This suggests an electron population far from the thermodynamic equilibrium. Based on the background pressure, the number of collisions with neutral xenon atoms experienced by a xenon ion and an electron was respectively estimated to be between one and three, and around one. Such regime is not collisionless, but not highly collisional either.

The electron cooling in a nearly-collisionless plasma is far from trivial, but the presented considerations on the EEPFs properties could serve as input and/or testing parameters for the modelling of the plume expansion.

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References

Boeuf J P 2017 J. Appl. Phys. 121 011101
Boyd I D and Dressler R A 2002 J. Appl. Phys. 92 1764–74
Dannenmayer K, Kudrpa, Tichy M and Mazouffre S 2012 Plasma Sources Sci. Technol. 21 055020
Dannenmayer K and Mazouffre S 2013 Plasma Sources Sci. Technol. 22 035004
Gudmundsson J T 2001 Plasma Sources Sci. Technol. 10 76–81
Gudmundsson J T 2001 Plasma Sources Sci. Technol. 10 76–81
Mazouffre S 2016 Plasma Sources Sci. Technol. 25 033002